# Structural Properties of Transition Metal Pyroarsenates $M_2As_2O_7$ (M = Co, Mn, Ni)

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Single phase powder samples of the transition metal pyroarsenates,  $M_2As_2O_7$  (M = Co, Mn, Ni), have been prepared and analyzed by X-ray diffraction, chemical analysis, high resolution powder neutron diffraction, and differential scanning calorimetry measurements. Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> were found to undergo high temperature structural phase transitions between  $\alpha$ - and  $\beta$ -forms at 452 and 691 K, respectively. The high temperature  $\beta$ -modifications of Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> are isomorphous with  $Sc_2Si_2O_7$  (thortveitite) of space group C2/m, with cell constants a = 6.6316(1) Å, b = 8.5541(1) Å, c = $4.7633(1) \text{ Å}, \beta = 103.56(1)^{\circ}, \text{ and } a = 6.5391(1) \text{ Å}, b = 8.5007(1) \text{ Å}, c = 4.7437(1) \text{ Å}, \beta = 103.19(1)^{\circ},$ respectively. Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> does not exhibit a high temperature phase transition and adopts the thortveitite structure at room temperature; a = 6.7442(2) Å, b = 8.7545(3) Å, c = 4.8025(2) Å,  $\beta =$ 102.76(1)°. The structures of all three thortveitite phases have been refined, and positional and thermal parameters are given. The  $\alpha$ - $M_2$ As<sub>2</sub>O<sub>7</sub> (M = Co, Ni) are triclinic (P1 or  $\overline{P1}$ ) but the structures could not be refined satisfactorily from powder neutron data. © 1990 Academic Press, Inc.

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#### 1. Introduction

Crystals of composition  $X_2Y_2O_7$  (X = K, Rb, Ca, Sr, Cd, Mg, Ni, Co, Zn, Mn, Cu, Sc; Y = Cr, V, As, P, Si, S) belong to a small number of groups of related structures (1). Compounds where the ionic radius of the Y atom, r(Y), is less than 0.60 Å, crystallize into structures analogous to those of pyrochlore and weberite in which Y is octahedrally coordinated (2). In the remainder, Y occurs in tetrahedral coordination and the compounds tend to adopt ei-

ther the thortveitite (Sc<sub>2</sub>Si<sub>2</sub>O<sub>7</sub>) structure (3) (r(X) < 0.97 Å) or one of the so-called "dichromate" structures (r(X) > 0.97 Å) (1). In these cases the crystals may be formulated as ionic with  $X^{n+}$  as the cation and  $Y_2O_7^{n-}$ , in which two  $YO_4$  tetrahedra share an oxygen atom, as the anion. In the dichromate structures the anion occurs in an eclipsed configuration with a Y-O-Y angle of  $\sim 130^{\circ}$ , while in the thortveitite structure it is staggered with a Y-O-Y angle of 180°.

A number of pyroarsenates and pyrophosphates  $M_2^{II} Y_2 O_7$  (M = Ni, Mg, Co, Zn,Cu; Y = As, P) occur in two polymorphs; a low temperature  $\alpha$ -phase and a high temperature  $\beta$ -phase. The  $\beta$ -phase always adopts the thortveitite structure with a linear Y-O-Y group whereas the  $\alpha$ -phase is always a close modification of the thort-0022-4596/90 \$3.00

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veitite structure with a bent Y-O-Y linkage. There has been much interest in the nature of the  $\alpha-\beta$  structural phase transition in these compounds and its relation to the bridging oxygen of the Y-O-Y group (4).

In the present paper we describe the preliminary results of an investigation of the structural properties of  $M_2As_2O_7$  (M = Co, Mn, Ni). We note that the magnetic properties of these compounds (5),  $\alpha$ -Co<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (6) and Mn<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (7), have also been studied. The compounds are all antiferromagnetic, adopting a variety of low-temperature magnetic structures.

Previous attempts to produce pure powder samples of  $M_2As_2O_7$  (M=Ni, Co) have resulted in mixtures of metal arsenates (8). We have found a very simple way of avoiding this problem and the present paper reports the preparation and structural characterization of single phase samples of  $M_2As_2O_7$  (M=Co,Mn,Ni).

# 2. Experimental

### 2.1 Preparations

2.1(i) Nickel pyroarsenate. Nickel pyroarsenate was prepared by adapting the preparation of Taylor and Heyding (8). As<sub>2</sub>O<sub>5</sub> (6.75 g; 0.03 moles) and Ni(NO<sub>3</sub>)<sub>2</sub> (11.64 g; 0.04 moles) were carefully ground together and placed in a porcelain crucible. Small quantities of As<sub>2</sub>O<sub>5</sub> were sprinkled onto the top of the mixture in an effort to maintain a significant vapor pressure of As in the crucible, and so prevent the evaporation of As from the reaction mixture. The crucible was placed in a muffle oven at 900°C for 2 hr and then cooled to room temperature over 3 hr.

Addition of excess  $As_2O_5$  prevented the formation of arsenic-deficient impurities such as  $Ni_3(AsO_4)_2$ , as was formed from Taylor and Heyding's preparation (8). The powder was removed from the crucible and

washed with hot distilled water to remove excess unreacted As<sub>2</sub>O<sub>5</sub>, the suspension filtered and the solid dried in air. The product was a golden yellow microcrystalline powder.

2.1(ii) Cobalt pyroarsenate. Cobalt pyroarsenate was prepared by a similar method to that of the nickel analog. As<sub>2</sub>O<sub>5</sub> (14.69 g; 0.064 moles) and  $Co(NO_3)_2$  (17.64)g; 0.06 moles) were ground together and placed in a platinum crucible. Again, excess As<sub>2</sub>O<sub>5</sub> was sprinkled on the surface of the reactants in the crucible to prevent the formation of a pink, arsenic-deficient impurity, Co<sub>3</sub>(AsO<sub>4</sub>)<sub>2</sub>. The crucible was placed in a muffle oven at 900°C for 2 hr and then cooled at room temperature over 3 hr. After removal from the crucible, the product was washed with hot distilled water to remove excess As<sub>2</sub>O<sub>5</sub>. A dark purple microcrystalline powder resulted.

2.1(iii) Manganese pyroarsenate. Manganese pyroarsenate was prepared by heating a porcelain crucible containing synthetic krautite, HMnAsO<sub>4</sub>·H<sub>2</sub>O, in a muffle oven at 600°C for 4 hr (9). The sample of krautite had been prepared following the method of Buckley (5).

### 2.2 Characterization

Small quantities of the products prepared in Section 2.1 were analyzed by atomic absorption spectroscopy using a Perkin-Elmer 8000 spectrometer.

X-ray diffraction profiles of the samples were obtained using a Philips PW1729 diffractometer controlled by a Philips 1710 microprocessor and minicomputer. All patterns were recorded at room temperature using  $CuK\alpha$  radiation of wavelength 1.541 Å. Powder data were analyzed using the X-ray powder pattern least-squares refinement program REFCEL (10) on the Oxford University VAX Cluster computer. This program refines the cell constants and zero point for a given set of reflections and their  $2\theta$  angles.

TABLE I CHEMICAL ANALYSIS OF TRANSITION METAL PYROARSENATES  $M_2As_2O_7$ 

Metal	% $M$ by weight	% As by weight
Со	30.78(31.03)	39.12(39.43)
Ni	30.81(30.96)	40.38(39.43)
Mn	28.28(29.55)	41.08(40.31)

Differential scanning calorimetry (DSC) measurements were made on the samples using a Perkin-Elmer 7 Series thermal analysis system (Co and Ni compounds) and a DuPont 9000 thermal analyzer with a 910 DSC module (Mn compound), by members of the Characterisation and Measurement Group, ICI Chemicals and Polymers Ltd., Runcorn, U.K.

### 2.3 Powder Neutron Diffraction

Data were collected on the High Resolution Powder Diffractometer (HRPD) (11) at Rutherford Appleton Laboratory (RAL), Didcot, Oxon, U.K. About 7 g of each of the samples was contained in rectangular vanadium cans inside a RAL furnace with vanadium windows. Data were collected for Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> between times of flight of 30-130 msec (d-spacing range of 0.6-2.6 Å) at room temperature. High temperature profiles were obtained Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> at 250°C and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> at 500°C between times of flight of 30-130 msec. Room temperature profiles were also collected for Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> (between times of flight of 30-130 msec) and Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> between times of flight of 30-280 msec (d-spacing range of 0.6-5.6 Å). After heating in the furnace the nickel and cobalt compounds were examined by X-ray diffraction to ensure that they had not cooled into new structural phases or been contaminated at high temperatures. The X-ray profiles of both compounds were exactly the same as those obtained before the experiment. The diffraction profiles were normalized by fitting a polynomial to the incident background shape and refined using the Rietveld profile refinement technique (12) modified for a pulsed neutron source (13).

#### 3. Results

#### 3.1 Characterization

The analytical results for M<sub>2</sub>As<sub>2</sub>O<sub>7</sub> are given in Table I. The numbers in parentheses are the theoretical percentage weights.

The room temperature X-ray diffraction profiles of the three compounds are shown in Fig. 1. The lattice constants, determined using REFCEL (10), are given in Table II, and the indexing of the X-ray diffraction profiles of the samples is given in the Appendix. The diffraction profiles of Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, whose room temperature structures are considered to be isomorphous (8, 14), were indexed using a triclinic cell in accordance with the lattice given by Ozog et al. (14) for Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. The tetragonal cell for Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> proposed by Taylor and Heyding (8) was not used. The X-ray profiles they obtained were poorly defined since their sample appeared to be contaminated with other arsenates.

No powder diffraction data have been published to date for Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> so the X-

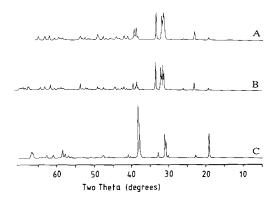
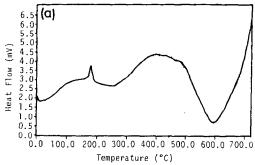


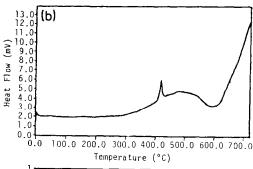
Fig. 1. Powder X-ray diffraction profiles of (a)  $Ni_2As_2O_7$ , (b)  $Co_2As_2O_7$ , and (c)  $Mn_2As_2O_7$ .

M	Space group	$a_0$	b <sub>0</sub> (Å)	$c_0$	α	β (°)	γ	No. of reflections fitted
Co	<i>P</i> 1	6.555(5)	8.521(5)	4.759(3)	91.00(4)	104.00(5)	91.29(3)	34
Mn	C2/m	6.745(8)	8.757(9)	4.803(7)	90.00	102.8(1)	90.00	22
Ni	<b>P</b> 1	6.558(8)	8.55(1)	4.712(5)	91.01(5)	103.98(7)	91.29(8)	37

TABLE II

Lattice Constants for M<sub>2</sub>As<sub>2</sub>O<sub>7</sub> at 300 K Determined by Powder X-Ray Diffraction





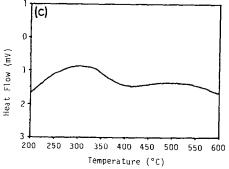


Fig. 2. DSC runs for (a)  $Co_2As_2O_7$ , (b)  $Ni_2As_2O_7$ , and (c)  $Mn_2As_2O^7$ .

ray diffraction profile was indexed using a C-centered monoclinic cell by analogy with Mn<sub>2</sub>P<sub>2</sub>O<sub>7</sub> and Mg<sub>2</sub>As<sub>2</sub>O<sub>7</sub> whose unit cells are monoclinic (15, 16).

The DSC scans for all three pyroarsenates are shown in Fig. 2 and Table III gives the conditions for the measurements and details of any peaks observed. The DSC scans for Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> reveal positive signals at around 452 and 692 K, respectively, corresponding to endothermic heat changes. The former has 2.85 kJ/mol and the latter 4.44 kJ/mol associated with it. No such peak is observed for Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub>.

### 3.2 Crystal Structure Refinement

Comparison between the high resolution powder neutron diffraction profiles obtained for the compounds  $M_2As_2O_7$  (M = Co, Mn, Ni) shows that for  $Co_2As_2O_7$  and  $Ni_2As_2O_7$ , a structural phase transition occurs on cooling from high to room temperature. This is probably associated with a lowering of the symmetry of the unit cell. The neutron diffraction profile of  $Mn_2As_2O_7$  at room temperature is very similar to those

TABLE III DIFFERENTIAL SCANNING CALORIMETRY RESULTS FOR  $M_2As_2O_7$  (M=Co,Mn,Ni)

M	$T_1$ (K)	T <sub>2</sub> (K)	T <sub>max</sub> (K)	Area (mJ)	$\Delta H$ (J/g)	ΔH (J/g)
Co	428.6	482.3	452.4	72.22	7,51	2.85
Ni	670.0	707.2	691.9	113.89	11.72	4.44

of  $Co_2As_2O_7$  and  $Ni_2As_2O_7$  at 250 and 500°C, respectively. This high resolution powder neutron diffraction data was used to refine the crystal structures of the  $M_2As_2O_7$  compounds.

# 3.2(i) High Temperature Phases of Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

The thortveitite structure was used as a starting model for the profile refinement of the high temperature structures of  $\text{Co}_2\text{As}_2\text{O}_7$  and  $\text{Ni}_2\text{As}_2\text{O}_7$  at 250 and 500°C, respectively (henceforth referred to as  $\beta\text{-Co}_2\text{As}_2\text{O}_7$  and  $\beta\text{-Ni}_2\text{As}_2\text{O}_7$ ).

The lattice dimensions and atom positions of Mg<sub>2</sub>As<sub>2</sub>O<sub>7</sub> (16) were used. The background was refined by fitting a fifth order Chebyschev polynomial. In both cases the program VDLSQ, which is contained in the Cambridge Crystallography Subroutine Library (CCSL) (17), was used. This program has as its peak shape function the convolution of a Gaussian with a Lorentzian (Voigt function) and two decaying exponential functions (18). The Voigt profile shape function was used to describe the significant peak broadening observed.

The refinements converged with  $\chi^2$  =  $3.4, R_n = 9.2\%, R_p = 4.6\%, \text{ and } R_{wp} = 5.8\%$ for  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and  $\chi^2 = 2.0$ ,  $R_n = 10.0\%$ ,  $R_{\rm p} = 3.6\%$ , and  $R_{\rm wp} = 4.5\%$  for  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> (terms described in Ref. (18)), using isotropic thermal factors. When the anisotropic thermal factors were allowed to vary, the fits improved in both cases to  $\chi^2 =$ 2.2,  $R_n = 6.9\%$ ,  $R_p = 3.7\%$ , and  $R_{wp} = 4.6\%$ for  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and  $\chi^2 = 1.5$ ,  $R_n = 6.1\%$ ,  $R_p = 3.2\%$ , and  $R_{wp} = 3.9\%$  for  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. Significance tests (19) indicated that the improvements in both cases were significant to 99.5% confidence limits. Large values of the anisotropic temperature factors  $B_{22}$  and  $B_{33}$  for the bridging oxygen, O1, of the  $As_2O_7$  group, were observed. The fits obtained are shown in Figs. 3 and 4. Tables IV and V contain structural data for the two compounds.

3.2(ii) Room Temperature Structure of Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

By analogy with Mn<sub>2</sub>P<sub>2</sub>O<sub>7</sub> and Mg<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, which also do not exhibit high temperature structural phase transitions, the space group of Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> was expected to be C2/m. All the observed peaks were indexed in this space group. Accurate unit cell constants of the monoclinic cell of Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> were obtained using the least-squares fitting program D5LSQ (CCSL) which refines unit cell constants for a given set of reflections and their times of flight.

The crystal structure of  $Mn_2As_2O_7$  was then refined by the Rietveld method for a pulsed neutron source using the program VDLSQ. The background was refined by fitting to a fifth order Chebyschev polynomial. Anisotropic temperature factors were again used for all the atoms in the unit cell. The refinement converged at  $\chi^2 = 12.6$ ,  $R_n = 13\%$ ,  $R_p = 7.8\%$ , and  $R_{wp} = 9\%$ . Anisotropic temperature factors  $B_{22}$  and  $B_{33}$  for the bridging oxygen O1 of the  $As_2O_7$  group were found to be large. The fit obtained is given in Fig. 5 and structural data in Tables VI and VII.

That the refinement converged to rather higher R-factors than is usual is probably due to anisotropic peak broadening that is not satisfactorily modeled by the Voigt function. Lowering the symmetry of the unit cell did not improve the fit. Furthermore, comparison of the  $F_{\rm obsd}$  and  $F_{\rm calcd}$  Fourier sections revealed that no scattering density was unaccounted for. Hence, the refinement is considered to be a solution of the structure although the fit is limited by sample effects.

# 3.2(iii) Room Temperature Structures of $Co_2As_2O_7$ and $Ni_2As_2O_7$

The room temperature powder neutron diffraction profile indicates that the unit cell of  $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> has lower symmetry than that of  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. Furthermore, Ozog *et* 

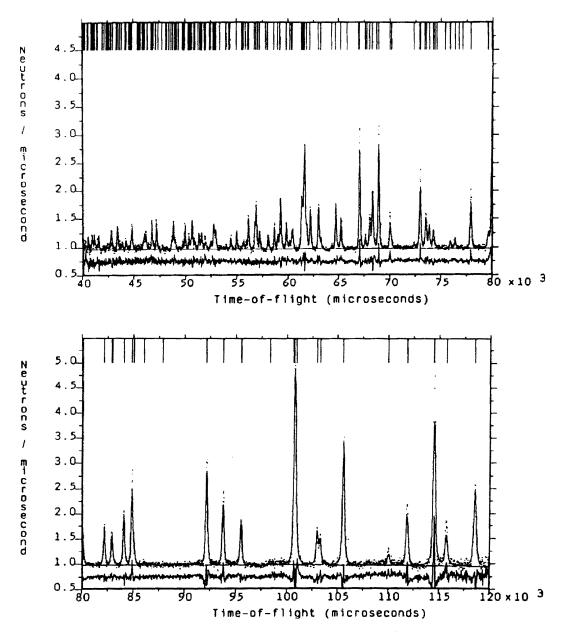


Fig. 3. Observed (dots) and calculated (full line) neutron diffraction profiles of  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. Lower line is difference and tags mark positions of reflections.

al. (14) obtained Weissenberg photographs from a single crystal of  $Co_2As_2O_7$  at room temperature and concluded that the unit cell was triclinic (C1 or C1). Hence, the starting model was deduced from the  $\beta$ -

 $Co_2As_2O_7$  unit cell (C2/m) by removing all the elements of symmetry and thereby creating 22 atom positions and the lattice constants obtained by Ozog *et al.* (14). The best fit had  $\chi^2 = 11$ ,  $R_n = 27\%$ ,  $R_p = 11\%$ ,

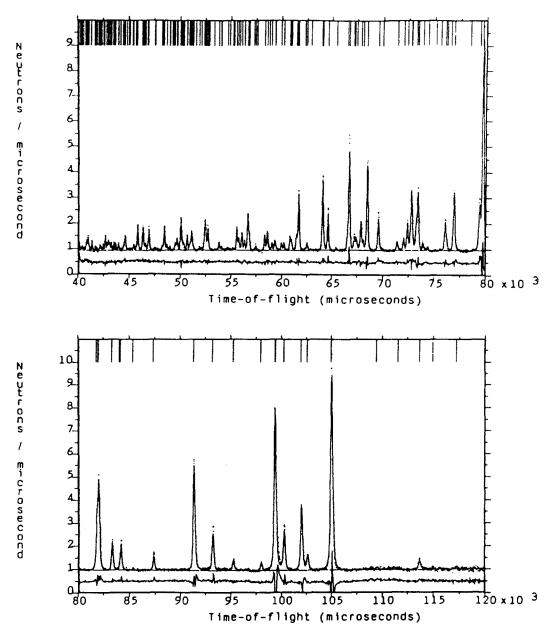


Fig. 4. Observed (dots) and calculated (full line) neutron diffraction profiles of  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. Lower line is difference and tags mark positions of reflections.

and  $R_{\rm wp} = 12\%$ . The intensities of the majority of peaks were incorrect. Furthermore, there were some observed peaks not predicted by the structural model given above. The latter were not considered to be

due to an impurity because the 250°C neutron profile and the X-ray pattern after the experiment showed no evidence of any.

Further attempts were made to deduce the space group and unit cell constants of

TABLE IV CRYSTALLOGRAPHIC DATA FOR  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

β-Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> β-Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> C2/mC2/mSpace group a = 6.6316(1) Åa = 6.5391(1) ÅAxes b = 8.5541(1) Åb = 8.5007(1) Åc = 4.7633(1) Åc = 4.7437(1) Å $\beta = 103.56(1)^{\circ}$  $\beta = 103.19(1)^{\circ}$ Positional parameters (a)  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>  $B_{\rm iso}~({\rm \AA}^2)$ y/bz/c0.3123(4) 0.2(1)Co 0.9047(3) 0.2246(2) -1.07(3)0 As 01 0 0.09(3)0.2252(3) -0.37(4) O2 0.3960(2)0.1620(1) 0.2310(2)0.7130(2)0.09(3) $O_3$ (b) β-Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> Ni 0.3136(1) 0.5 0.17(3)0.2263(2) 0 0.9030 -0.73(3)As 01 O 6.9(1)O2 0.3983(2)0.2303(3)0.32(4)0.1648(1) 0.7129(2) 03 0.2315(2)0.80(4)Anisotropic thermal factors for β-Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> Atom  $B_{33}$  $B_{23}$  $B_{13}$  $B_{12}$  $\boldsymbol{B}_{11}$  $B_{22}$ Co 1.8(2) 0.5(2)3.2(2) 0 0.2(1)0 0.6(1)0.6(1)0.4(1) 0 -0.11(5)0 As 8.2(3) 2.0(1)O(1) 1.3(2)16.1(4) A Û 2.40(9) 0.93(7)0.73(7)0 -0.24(7)0 O(2) 3.36(7) 0.85(5)0.24(4)0.32(4)0.65(6) O(3)1.42(5)Anisotropic thermal factors for β-Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> Atom  $B_{11}$  $B_{22}$  $B_{33}$  $B_{23}$  $B_{13}$  $B_{12}$ 1.74(4) Ni 2.14(4)0.91(4)0 -0.20(3)0 As 1.07(5) 0.86(6)0.44(6)0 -0.65(5)0 O(1) 1.9(2) 14.0(4) 10.7(3) 2.1(1) 0 -0.56(6)0 O(2) 2.65(8)1.16(7)0.67(6)3.20(6) 1.66(5) 1.74(6) 0.79(4)0.25(4)0.46(4)

 $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. The extra peaks could not be indexed in space groups P1 or  $P2_1/c$  with the original C2/m cell constants. Combinations of doubled unit cell constants in space group P1 were tried but none of these trials would account for the unpredicted observed peaks. The autoindexing program of Visser (20) yielded no sensible solutions for 30 reflections between times of flight of 60–

Note. The temperature factor has the form  $\exp[-\frac{1}{4}\{B_{11}h^2a^{*2} + \dots]]$ 

 $2B_{12}hka*b* + . . .}$ 

TABLE V Interatomic Distances for  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

Atoms	Bond length (Å)	Atoms	Bond angle (°)
	β-Co <sub>2</sub> A	As <sub>2</sub> O <sub>2</sub>	
As <sub>2</sub> O <sub>2</sub> group	p 002	10207	
As-Ola	1.656(2)	O1-As-O2	102.2(1)
As-O2a	1.676(2)	O1-As-O3	106.89(7)
As-O3	1.666(1)	O2-As-O3	113.60(6)
		O3-As-O3	112.6(1)
		As-O1-As	180.0(0)
O1~O2	2.594(1)		
O1~O3b	2.668(1)		
O2~O3c	2.790(2)		
$O3-O3^{d}$	2.772(2)		
CoO6 group			
Co~O2e	2.084(3)	O2-Co-O3	151.96(8)
Co-O3	2.074(2)	O2-Co-O3	79.80(8)
Co~O3e	2.260(1)	O2-Co-O2	79.2(1)
		O2-Co-O3	94.16(4)
Co-Cod	3.211(7)	O3CoO3	168.8(2)
		O3-Co-O3	114.26(8)
		Co-O2-Co	100.8(1)
		Co-O3-Co	106.88(5)
	β-Ni <sub>2</sub> A	AS <sub>2</sub> O <sub>7</sub>	
As <sub>2</sub> O <sub>7</sub> group			
As-O1a	1.647(1)	O1-As-O2	101.22(9)
As-O2a	1.697(1)	O1-As-O3	106.33(7)
As-O3	1.671(1)	O2-As-O3	113.77(6)
		O3-As-O3	114.0(1)
		As-O1-As	180.0(0)
O1-O2	2.584(1)		
O1-O3b	2.655(1)		
O2~O3c	2.756(2)		
O3~O3 <sup>d</sup>	2.802(2)		
NiO <sub>6</sub> group			
Ni-O2 <sup>e</sup>	2.050(1)	O2-Ni-O3	151.79(5)
Ni-O3	2.053(1)	O2-Ni-O3	80.21(5)
Ni-O3 <sup>e</sup>	2.224(1)	O2-Ni-O2	78.75(6)
		O2-Ni-O3	94.10(3)
Ni-Nid	3.169(2)	O3-Ni-O3	170.53(6)
		O3-Ni-O3	113.42(5)
		Ni-O2-Ni	101.25(6)
		Ni-O3-Ni	107.20(4)

*Note.* Equivalent positions: (a) x, y, z + 1; (b) x, y, -z; (c) -x, y, -z; (d) x, -y, z; (e)  $-(x + \frac{1}{2}), -y + \frac{1}{2}, z$ .

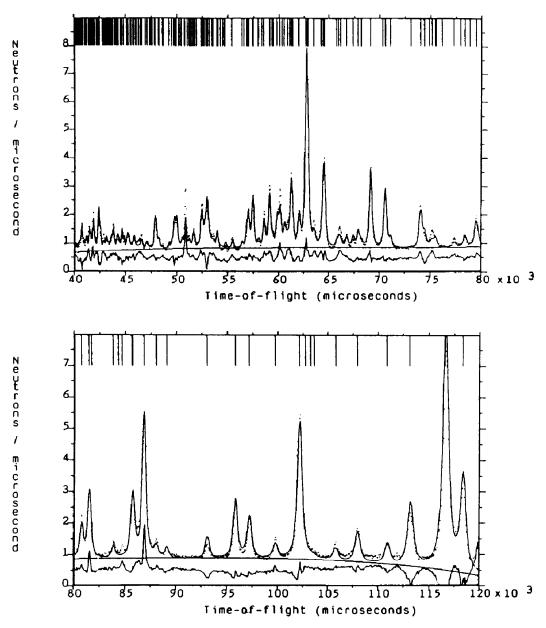


Fig. 5. Observed (dots) and calculated (full line) neutron diffraction profiles of  $Mn_2As_2O_7$  using Voigt profile function and anisotropic thermal factors. Lower line is difference and tags mark the positions of the reflections.

140 msec. In an attempt to measure the low order reflections and thereby deduce the unit cell, a neutron diffraction profile was obtained at longer times of flight, 140-280

msec (i.e., greater *d*-spacing; 2.8-5.6 Å). No extra reflections were observed that could not be indexed on the original triclinic unit cell.

TABLE VI
CRYSTALLOGRAPHIC DATA FOR Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

Space group Axes		$C2/m$ $a = 6.$ $b = 8.$ $c = 4.$ $\beta = 10$		
Atom	x/a	y/b	z/c	$B_{\rm iso}$ (Å <sup>2</sup> )
Mn	0	0.3110(4)	0.5	1.1(2)
As	0.2268(3)	0	0.9062(7)	-0.2(1)
01	0	0	0	6.4(4)
O2	0.3977(5)	0	0.2156(8)	-0.7(1)
O3	0.2336(3)	0.1582(3)	0.7107(6)	0.18(9)

Atom	$B_{11}$	$B_{22}$	$B_{33}$	$B_{23}$	$B_{13}$	B <sub>12</sub>
Mn	0.00	-1.7(2)	9.7(5)		-1.9(3)	
As	-2.1(1)	1.0(1)	2.2(2)		-0.5(1)	
O1	0.8(3)	14.7(8)	8.1(6)		5.4(3)	
O2	0.1(1)	-0.1(1)	2.8(2)		-2.5(2)	
O3	-0.6(1)	0.3(1)	4.2(2)	0.00	-2.0(1)	0.8(1)

*Note*. The temperature factor has the form  $\exp[-\frac{1}{4}\{B_{11}h^2a^{*2} + \dots 2B_{12}hka^*b^* + \dots]\}$ .

Atoms	Bond length (Å)	Atoms	Bond angle (°)
As <sub>2</sub> O <sub>7</sub> group			
As-O1a	1.687(3)	O1-As-O2	104.5(9)
As-O2a	1.67(3)	O1-As-O3	106.7(1)
As-O3	1.679(3)	O2-As-O3	113.5(4)
		O3-As-O3	111.1(3)
		As-O1-As	180.0(0)
O1-O2	2.635(3)		
O1-O3b	2:715(3)		
O2-O3c	2.794(4)		
$O3-O3^d$	2.783(4)		
MnO <sub>6</sub> group			
Mn-O2e	2.16(2)	O2-Mn-O3	151.2(4)
Mn-O3	2.143(3)	O2-Mn-O3	78.5(6)
Mn-O3e	2.265(3)	O2-Mn-O2	80(1)
		O2-Mn-O3	94.6(4)
$Mn-Mn^d$	3.309(7)	O3-Mn-O3	166.3(2)
		O3-Mn-O3	115.9(1)
		Mn-O2-Mn	100(1)
		Mn-O3-Mn	106.7(1)

*Note*. Equivalent positions: (a) x, y, z + 1; (b) x, y, -z; (c) -x, y, -z; (d) x, -y, z; (e)  $-(x + \frac{1}{2}), -y + \frac{1}{2}, z$ .

The structure of  $\alpha$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> was considered to be isomorphous with that of  $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> (8). Furthermore, the X-ray diffraction profiles of the two compounds are very similar (Fig. 1). As was the case for  $\alpha$ - $Co_2As_2O_7$ , the structure of  $\alpha$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> was considered to be closely related to that of thortveitite but of lower symmetry. The same starting model as used for  $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> was employed in the refinement. The refinement converged with very large R-factors,  $R_n = 26\%$ ,  $R_p = 13\%$ , and  $R_{wp} = 16\%$ , for reasons similar to those that prevented full refinement of the  $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> data. The predicted intensities of the model were too low for most reflections and some observed peaks were not predicted by the model.

The similarity between the fits indicates that both structures are closely related to their high temperature analogs and hence to the parent compound thortveitite. The presence of unpredicted peaks in both refinements indicates that the unit cell and space group are incorrect, although the symmetry is unlikely to be anything other than triclinic, as the structure is clearly almost correct. It would appear that some subtle combination of any number of the unit cell axes has occurred. In the future we intend to obtain high resolution X-ray diffraction profiles of  $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>  $\alpha$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> in order to measure the lowest order reflections which are not obtainable using HRPD. It may then be possible to establish the unit cells of the compounds by auto-indexing methods.

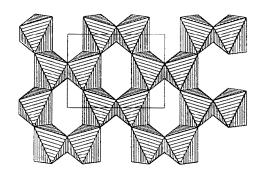
#### 4. Discussion

For the first time we have prepared single phase samples of the transition metal pyroarsenates,  $M_2As_2O_7$  (M = Co, Mn, Ni). A previous attempt to prepare them resulted in mixtures that were at least biphasic (8) and this lead to an incorrect assignment of the unit cell from powder X-ray diffraction data. In the present work powder X-ray dif-

fraction profiles have been successfully indexed on the basis of monoclinic  $(Mn_2As_2O_7)$ and triclinic ( $\alpha$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, α-Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>) unit cells, although the full crystal structures of the latter two compounds remain to be established. Powder neutron diffraction experiments shown that Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> undergo high temperature structural phase transitions in common with other  $M_2X_2O_7$ compounds. Endothermic signals in the DSC traces of Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> are observed at 452 and 691 K, respectively, and almost certainly correspond to the  $\alpha$ - $\beta$ -phase transition.

# 4.1 The Crystal Structures of $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, and Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

We have shown that  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>,  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, and Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> are isomorphous and adopt the thortveitite structure, of which Sc<sub>2</sub>Si<sub>2</sub>O<sub>7</sub> is the parent compound. The essential features of the structure are as follows: the  $M^{2+}$  (M = Co, Mn, Ni) octahedra share edges in a hexagonal arrangement in the ab-plane, as depicted in Fig. 6, forming a distorted honeycomb arrangement of  $M^{2+}$  ions. The arsenate sheets are packed in such a way that an As ion on one side of the As<sub>2</sub>O<sub>7</sub> group shares one oxygen atom from the NiO<sub>6</sub> sheet above and two oxygen atoms from the NiO<sub>6</sub> below, in the



Ftg. 6. Projection on the (0 0 1) plane of  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>,  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, and Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> showing the hexagonal arrangement of MO<sub>6</sub> octahedra.

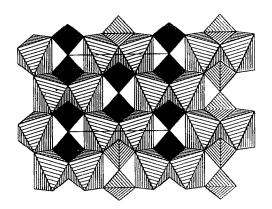


Fig. 7. Projection on the (0 0 1) plane of  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>,  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, and Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> showing the hexagonal arrangement of MO<sub>6</sub> octahedra and AsO<sub>4</sub> tetrahedra (shaded).

z-direction. The  $As_2O_7$  groups are in a staggered conformation (Figs. 7 and 8) so that the As ion from the opposite side of the  $As_2O_7$  group shares two oxygens above and one below in the z-direction. Adjacent  $MO_6$  octahedra along the b-axis share a pair of O2 atoms with distances of 2.050(1) Å (Ni-O2), 2.084(3) Å (Co-O2), and 2.16(2) Å (Mn-O2). The coordination octahedra are tetragonally elongated along the a-axis with (M-O3) bond lengths of 2.224(1) Å (Ni-O3), 2.260(1) Å (Co-O3), and 2.265(3) Å (Mn-O3). The remaining M-O bond lengths are 2.053(1) Å (Ni-O3), 2.074(2) Å (Co-O3), and 2.143(3) Å (Mn-O3).

The pyroarsenate anion consists of corner-shared tetrahedra with the bridging oxygen (O1) to arsenic distance, 1.647(1) Å (M = Ni), 1.656(2) Å (M = Co), and 1.687(3) Å (M = Mn). The As-O2 bond lies in the mirror plane and has a length of 1.697(1) Å (M = Ni), 1.676(2) Å (M = Co), and 1.67(3) Å (M = Mn). The remaining unique As-O bond length is 1.671(1) Å (M = Ni), 1.666(1) Å (M = Co), and 1.679(3) Å (M = Mn).

We note that  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> is isomorphous with  $\beta$ -Ni<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (21). It is interesting that three low temperature forms of Ni<sub>2</sub>P<sub>2</sub>O<sub>7</sub> are

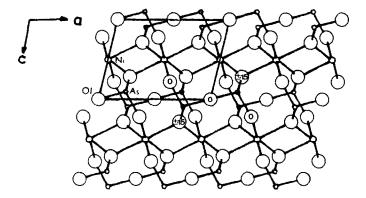


Fig. 8. Crystal structure of  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub>,  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>, and Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub>. The atomic positions in one pyroarsenate group are marked.

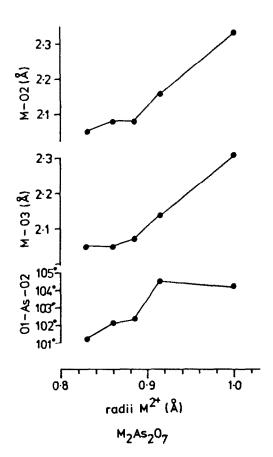


Fig. 9. Metal-oxygen bond lengths and O1-As-O angles for a series of transition metal pyroarsenates.

known;  $\gamma$ -Ni<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (22),  $\sigma$ -Ni<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (23), and  $\alpha$ -Ni<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (22). In the  $\sigma$ -form the O–P–O bond is linear.

# 4.2 High Temperature Structural Phase Transitions

Figure 9 shows metal-oxygen distances and O1-As-O angles for a series of transition metal pyroarsenates. In common with other structures of thortveitite analogs (e.g., 4, 16, 24) the terminal O-As-O bond angles are larger than expected for a perfect tetrahedron, e.g., O2-As-O3 in  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> is 113.6°, and the O-As-O angles including the bridging oxygen atom are smaller, e.g., O1-As-O2 in  $\beta$ -Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub> is 102.2°.

Two tetrahedral AsO<sub>4</sub> units may be connected by a linear As-O-As linkage. However, in this structure the geometry of the AsO<sub>4</sub> unit is governed by the bonding of the terminal oxygens to the metal ion. This means that to compensate for the linear As-O-As linkage, the AsO<sub>4</sub> groups must be compressed because the positions of the terminal oxygen atoms are primarily determined by the metal atoms and are therefore fixed. Furthermore, the shorter the M-O distance, the more distorted the AsO<sub>4</sub> tetrahedron and hence the greater the deviation of the terminal O-As-O1 bond angles from

109°. This is clearly in evidence in Fig. 9. The shortest M-O distances occur in those compounds with the smallest  $M^{2+}$  radius; for example,  $\beta$ -Ni<sub>2</sub>As<sub>2</sub>O<sub>7</sub> (Shannon and Prewitt (25), ionic radius Ni<sup>2+</sup> = 0.83 Å) has M-O2 = 2.05 Å and the O1-As-O2 angle is 101.2°. For larger metal ions such as Mn<sup>2+</sup> (ionic radius 0.97 Å (25)) the M-O bond lengths are greater (e.g., Mn-O2 = 2.16 Å in Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> at 104.5°, and the O2-As-O1 bond angle is less distorted from 109°.

It seems likely that the distortion of AsO<sub>4</sub> in the  $\beta$ -phase compounds may play some part in the  $\alpha$ - $\beta$ -phase transition, thus the compounds with large metal ions (e.g., Mn<sub>2</sub>As<sub>2</sub>O<sub>7</sub> and Ca<sub>2</sub>As<sub>2</sub>O<sub>7</sub>) have larger M-O distances and hence less distorted AsO<sub>4</sub> tetrahedra and do not exhibit the  $\alpha$ - $\beta$ -phase transition. It is those compounds with shorter M-O distances and more distorted AsO<sub>4</sub> tetrahedra that undergo the high temperature  $\alpha$ - $\beta$ -phase transition.

It is noteworthy that in all  $M_2As_2O_7$  the anisotropic thermal factors of the bridging oxygen of the As<sub>2</sub>O<sub>7</sub> group are large (Tables V and VII). Indeed, this behavior is observed for all  $\beta$ -phase pyroarsenates and pyrophosphates isomorphous with thortveitite. The origin of such large anisotropic temperature factors has been discussed in detail (e.g., 26). It may be due to either a dynamic or static positional disorder. If the former, there would be enhanced thermal motion with its major component in the bdirection, perpendicular to the As-As bond direction. If the latter, the anion would be bent so that in half the unit cells O1 is displaced from the center of symmetry along the positive y direction and in the remainder, along the negative y direction. To refine the structure of the  $\beta$ -phase in terms of a disordered structure requires a knowledge of the crystal structure of the  $\alpha$ -phase to generate the disordered structure.

It is apparent that the enhanced vibration of the bridging oxygen atom must play a key role in the  $\alpha-\beta$ -phase transitions of

metal pyroarsenates and pyrophosphates. In the low temperature ( $\alpha$ ) structures the X-O1-X (X = As or P) bond changes from a linear configuration in the  $\beta$ -phase to a bent one, e.g., 157° for  $\alpha$ -Cu<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (26) and 144° for  $\alpha$ -Mg<sub>2</sub>P<sub>2</sub>O<sub>7</sub> (27). So, the  $\alpha$ - $\beta$ -phase transition may be envisaged as a "freezing out" of the thermal motion of the bridging oxygen atom in a potential well causing a bent X-O-X linkage. Coupled with this, one of the crystallographically equivalent

TABLE A
X-Ray Powder Diffraction Pattern of
Co<sub>2</sub>As<sub>2</sub>O<sub>7</sub>

$I/I_{\text{max}} (\times 10)$	$d_{\mathrm{obsd}}$ (Å)	$d_{\mathrm{calcd}}(\mathring{\mathrm{A}})$	h	k	i
0.7	5.023	5.028	1	1	0
2.2	4.24	4.26	0	2	0
0.8	3.78	3.80	-1	1	1
9.5	3.15	3.17	1	-1	1
8.2	3.097	3.098	1	1	1
10.0	2.971	2.977	-2	0	1
1.1	2.616	2.619	1	-3	0
3.5	2.589	2.581	2	-2	0
0.7	2.569	2.566	1	3	0
2.7	2.53	2.51	2	2	0
0.1	2.448	2.444	0	-3	1
0.9	2.423	2.428	-2	-2	1
0.9	2.306	2.308	0	0	2
1.4	2.268	2.267	1	1	2
0.3	2.204	2.205	1	-3	1
0.4	2.147	2.147	0	4	0
1.0	2.080	2.077	- i	-2	2
2.0	2.063	2.064	-2	1	2
0.6	1.919	1.919	-3	2	1
2.9	1.897	1.894	-3	-2	1
1.6	1.741	1.740	-2	4	1
0.8	1.721	1.722	3	1	1
0.9	1.695	1.691	-3	-3	1
2.2	1.669	1.668	1	3	2
1.9	1.632	1.634	1	5	0
1.7	1.603	1.606	-4	1	1
1.6	1.538	1.539	0	0	3
1.2	1.518	1.519	2	-5	0
0.9	1.508	1.508	-2	-4	2
1.3	1.429	1.428	2	3	2
0.7	1.419	1.419	1	0	3
1.5	1.390	1.390	4	-1	1
0.9	1.375	1.375	-3	4	2

TABLE B X-Ray Powder Diffraction Pattern of  $Ni_2As_2O_7$ 

TABLE C X-Ray Powder Diffraction Pattern of  $Mn_2As_2O_7$ 

$I/I_{\text{max}} (\times 10)$	d <sub>obsd</sub> (Å)	d <sub>calcd</sub> (Å)	h	k	l
0.6	4.94	5.04	1	1	0
1.9	4.16	4.23	-1	0	1
0.4	3.72	3.78	<b>-1</b>	1	1
10.0	3.12	3.15	1	<b>— 1</b>	1
7.1	3.07	3.08	1	1	1
7.6	2.94	2.95	2	1	0
1.1	2.751	2.753	1	3	0
2.8	2.51	2.52	2	2	0
1.2	2.41	2.43	-2	-2	1
1.4	2.36	2.36	2	0	1
0.6	2.29	2.29	2	-1	1
1.3	2.255	2.253	2	1	1
0.4	2.194	2.195	0	1	2
0.6	2.131	2.131	-3	0	1
1.2	2.100	2.093	2	3	0
0.5	1.963	1.962	1	-1	2
0.7	1.948	1.953	0	-4	1
0.9	1.921	1.921	3	-2	0
0.6	1.898	1.898	-2	-2	0
1.2	1.877	1.879	3	2	0
0.4	1.759	1.762	0	3	2
0.8	1.736	1.742	3	-1	1
1.0	1.709	1.709	0	5	0
0.8	1.680	1.679	3	3	0
0.2	1.648	1.650	-3	2	2
1.6	1.620	1.616	1	3	2
1.0	1.582	1.579	0	-4	2
0.8	1.508	1.509	-3	-3	2
1.0	1.505	1.505	-2	-4	2
1.3	1.493	1.494	0	1	3
0.9	1.484	1.485	<b>-4</b>	0	2
0.7	1.386	1.386	-1	-3	3
1.1	1.379	1.375	4	1	1
0.6	1.364	1.365	-1	3	3
0.5	1.335	1.337	-3	2	3
0.6	1.321	1.322	-4	3	2
0.6	1.276	1.276	-1	-4	3

$I/I_{\rm max}~(\times~10)$	$d_{\mathrm{obsd}}$ (Å)	$d_{\mathrm{calcd}}$ (Å)	h	k	l
1.2	5.13	5.26	1	1	0
0.2	4.32	4.38	0	2	0
0.2	3.28	3.29	2	0	0
0.8	3.21	3.23	1	1	1
1.1	3.19	3.20	0	2	1
0.2	3.02	3.02	2	0	-1
0.3	2.662	2.668	1	3	(
10.0	2.625	2.630	2	2	0
0.1	2.485	2.489	2	2	-1
0.2	2.448	2.449	2	0	1
0.05	2.230	2.234	1	3	1
0.1	2.124	2.127	3	1	0
0.2	1.803	1.822	2	4	(
0.1	1.797	1.797	3	1	1
0.1	1.773	1.773	2	4	-1
0.3	1.752	1.753	3	3	(
0.2	1.687	1.687	1	3	2
0.1	1.645	1.644	4	0	(
0.3	1.562	1.562	0	0	3
0.4	1.555	1.554	3	3	1
0.2	1.381	1.380	4	2	1
0.2	1.368	1.365	3	5	-1

 $M^{2+}$  ions may change from six- to fivefold coordination of oxygen ions. The phase transition involves a lowering of the crystal symmetry accompanied by enlargement of one or two of the unit cell axes. Thus for  $M_2'X_2O_7$  (M' = Cu, X = P; M' = Mg, X = P; M' = Zn, X = As), the c-axis is doubled on going from the  $\beta$ -phase to the  $\alpha$ -phase

while the a-axis is unchanged, doubled and tripled, respectively (26, 28, 29). Since the structures of the  $\alpha$ -forms of  $Co_2As_2O_7$  and  $Ni_2As_2O_7$  have not yet been determined fully, it is difficult to envisage possible mechanisms for the  $\alpha$ - $\beta$ -phase transition in these compounds. However, by analogy with other  $\alpha$ -phase compounds, some multiplying of the unit cell axes must occur and the As-O-As linkage is likely to be bent.

## **Appendix**

Tables of X-ray powder diffraction data for  $M_2As_2O_7$ ; M = (a) Co, (b) Ni, and (c) Mn, at room temperature.

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